

Solid-state amorphization of Cu nanolayers embedded in a $\text{Cu}_{64}\text{Zr}_{36}$ glass

Tobias Brink,^{*} Daniel Şopu,[†] and Karsten Albe

*Fachgebiet Materialmodellierung, Institut für Materialwissenschaft,
Technische Universität Darmstadt, Jovanka-Bontschits-Str. 2, D-64287 Darmstadt, Germany*

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Solid-state amorphization of crystalline copper nanolayers embedded in a $\text{Cu}_{64}\text{Zr}_{36}$ metallic glass is studied by molecular dynamics simulations for different orientations of the crystalline layer. We show that solid-state amorphization is driven by a reduction of interface energy, which compensates the bulk excess energy of the amorphous nanolayer with respect to the crystalline phase up to a critical layer thickness. A simple thermodynamic model is derived, which describes the simulation results in terms of orientation dependent interface energies. Detailed analysis reveals the structure of the amorphous nanolayer and allows a comparison to a quenched copper melt, providing further insights into the origin of excess and interface energy.

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I. INTRODUCTION

Metals show a strong tendency to form crystalline phases and only appear in an amorphous state under certain conditions. Using far-from-equilibrium processes, metals can be kinetically trapped in a metastable state. This includes bulk metallic glasses (BMG), which are highly alloyed metallic systems quenched from the melt. The glass formation is supported by rapid quenching and the size difference of the component atoms.^{1–3} Furthermore, a crystalline metal sample can be forced into a disordered state by ion irradiation. The disorder is introduced by high-energy impacts of ions, which disturb the ordered lattice due to local melt-quench processes.⁴ Thin films produced with high deposition rates can also be amorphous.⁵ In this case, the amorphous state is metastable and only induced due to the high growth rate in the deposition process, while in equilibrium thin metal films on a variety of substrates usually are crystalline. Examples include iron on amorphous carbon substrates;⁶ Cu, Ag, Al, Au, and Ni on sapphire substrates;^{7–9} and Ni on tungsten substrates¹⁰ among many others. Amorphization is not limited to far-from-equilibrium processes, but can also happen for purely energetic reasons. High-angle, high-energy grain boundaries in some polycrystalline metal systems exhibit an amorphous structure due to the misorientation of the neighboring crystal lattices.¹¹ Molecular dynamics (MD) computer simulations on single-component¹² and binary alloy¹³ Lennard-Jones systems identify a nanocrystalline instability. Nanocrystalline materials with grain sizes smaller than a critical value become unstable and collapse completely, leaving behind an amorphous metal, i.e., the grain boundary phase. Similarly, metallic nanoparticles below a critical size can also occur in an “amorphous” phase driven by the reduction of surface energy.¹⁴

In heterogeneous interfaces between crystalline metals, amorphous interphases were also found.¹⁵ These inter-

face interphases are thermodynamically stable and result from the misorientation and lattice mismatch between the adjacent crystallites.^{16,17} This effect is called solid-state amorphization (SSA) and has recently also been discussed in the framework of complexion formation.¹⁸ Similar to the formation of interface interphases, a thin metallic film embedded in a different crystal phase can transform into an amorphous state if the thickness is below a critical value.^{19–21} While energetically driven amorphization of a thin crystalline layer due to size mismatch and misorientation to the abutting crystalline phases is a well known phenomenon, the amorphization of a thin elemental metal layer embedded in an amorphous matrix appears to be less likely, since the driving force should be significantly smaller.

Ghafari *et al.*, however, showed recently that iron nanolayers embedded in an amorphous glass ($\text{Co}_{75}\text{Fe}_{12}\text{B}_{13}$) can become amorphous, if the thickness is five monolayers (ML) or less, while at six or more monolayers a crystalline phase is observed.²² Whether or not this is a kinetic effect due the deposition conditions or an energetically driven phenomenon, which might depend on the lattice orientation, is the problem of interest in this study.

In order to address this, we conducted MD simulations of Cu nanolayers of different orientation embedded in a $\text{Cu}_{64}\text{Zr}_{36}$ matrix and investigated the driving force behind the amorphization. Since there is no adequate iron alloy potential which also correctly models an alloy that forms a metallic glass (MG), we instead used a system based on Cu and Zr. To investigate the thermodynamic stability of the amorphous layer, we start from crystalline nanolayers of varying thickness and check if there is a phase transition to the amorphous state at a critical thickness. We then develop a simple thermodynamic model based on the assumption that any amorphization in this setup must be energetic in nature and check it against our simulation results.

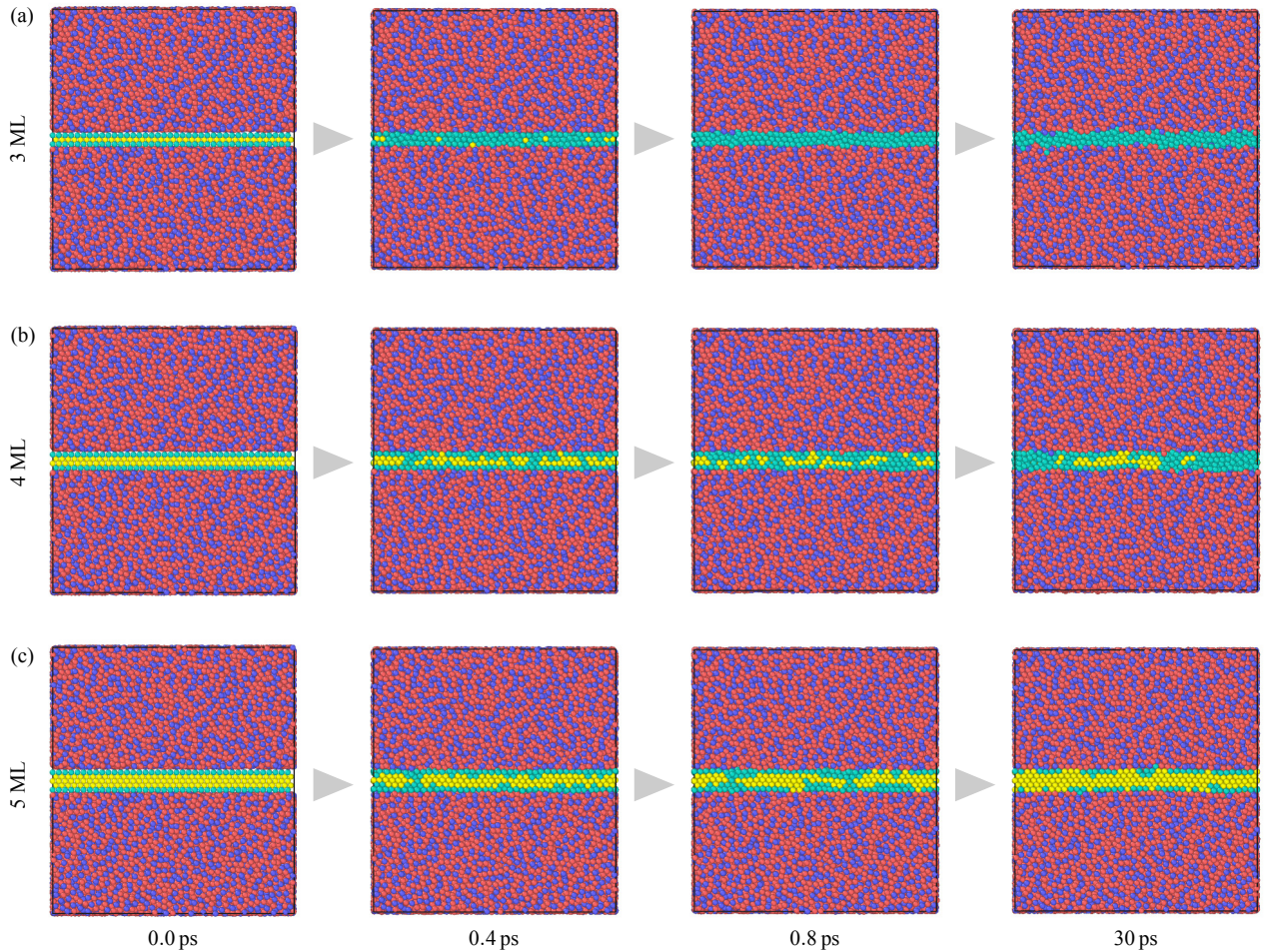


FIG. 1. Time evolution of the composite $\text{Cu}_{64}\text{Zr}_{36}$ -Cu systems with different nanolayer thickness. Exemplarily, we show a system in which a copper nanolayer with fcc (100) surface was inserted. The top row (a) shows the evolution of the system with a copper nanolayer thickness of three monolayers. The nanolayer in this system amorphizes almost immediately. The middle row (b) depicts a system with four monolayers of copper, which stay partly crystalline. The bottom row (c) contains snapshots of a system where the nanolayer has a thickness of five monolayers. Here, the nanolayer stays crystalline. This simulation used the Mendelev potential. Copper atoms are shown in red, zirconium atoms in blue. Copper atoms that belong to the inserted layer are green, except for those in fcc configuration, which are shown in yellow.

II. SIMULATION METHODS AND SAMPLE PREPARATION

A. Simulation method

We conducted MD simulations using LAMMPS.²³ The potential energy was modelled by a Finnis-Sinclair type potential by Mendelev *et al.*,²⁴ which was mostly fitted to the glassy state, and another potential by Ward *et al.* This second potential consists of elemental potentials by Zhou *et al.*²⁵ that were combined into an alloy potential by fitting to several intermetallic phases using the Ward method.²⁶ To obtain independent confirmation of our simulation results, we ran simulations with both potentials. The time-step length was set to 2 fs. In all simulations we employed periodic boundary conditions to obtain a surface-free system.

B. Sample preparation

$\text{Cu}_{64}\text{Zr}_{36}$ metallic glasses were prepared by quenching from the melt at 2000 K to 300 K with a cooling rate of 0.01 K/ps. This procedure yields a MG with a local topology matching the experiment.^{27,28} Two glasses with 63108 atoms were prepared, one using the Mendelev potential and one using the Ward potential. The final size of the simulation box is approximately $10 \times 10 \times 10 \text{ nm}^3$. All following steps were carried out twice, once with the Mendelev and once with the Ward potential.

Copper nanolayers with the appropriate lattice constants at 300 K were created with (100), (110), and (111) surfaces. For each of these, the thickness varies between 2 ML and 15 ML. To avoid stresses in the nanolayers after insertion into the glass matrix, we scaled the x and y

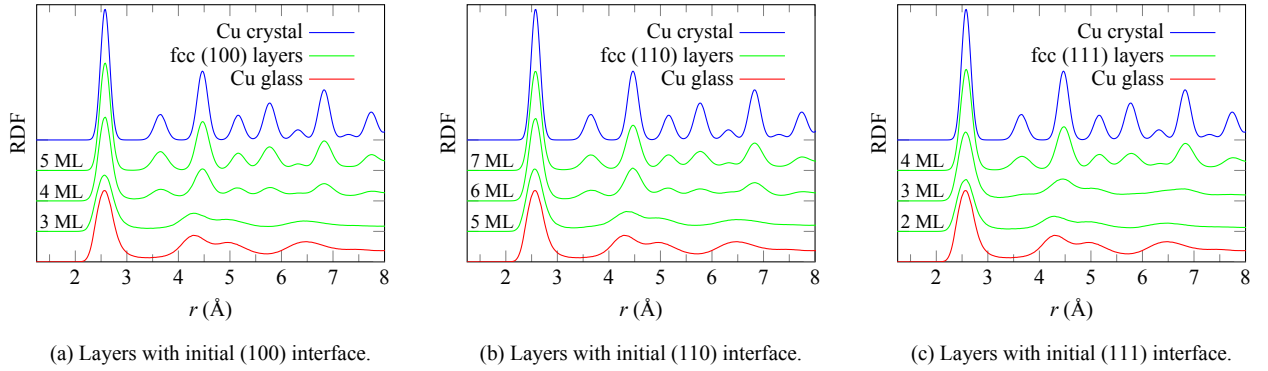


FIG. 2. Radial distribution functions of the copper nanolayers in several composite systems compared with the reference systems. Results of the simulation carried out using the Mendelev potential.

dimensions of the glass to fit the nanolayers exactly and relaxed it again with a barostat applied in z direction at ambient pressure for 1 ns.

The glass was cut at an arbitrary xy plane and the copper layers were inserted, so that the minimum initial distance between any nanolayer atom and any matrix atom was at least 1.5 Å. The possible consequences of low atomic distance and the resulting high potential energy at the interface are discussed later in section IV A. To develop a stable interface, the systems were equilibrated for 1 ns at 300 K, again with a barostat applied only in the z direction. We kept the lateral dimensions constant because any change in them would be dominated by the relaxation of the MG. This would induce unwanted stresses in the nanolayer. At the end of this procedure, the systems were completely equilibrated (cf. 29, section I).

Further, we created reference systems of crystalline and amorphous copper phases. For the crystalline phase, we simply equilibrated fcc copper at 300 K to obtain the correct lattice constant. Bulk amorphous copper was obtained by quenching from the melt at 2000 K with very high cooling rates. We had to employ a cooling rate of 1 K/ps for the Mendelev potential and 25 K/ps for the Ward potential. These cooling rates are approximately the minimum cooling rates needed to avoid crystallization. The difference is a result of the different glass-forming ability of elemental copper in the two potentials.

C. Analysis

We applied a common neighbor analysis (CNA)^{30,31} as implemented in OVITO³² to identify the structure of the nanolayers in the composite. The CNA calculates the coordination of all atoms by examining their neighborhood. To confirm these results, we calculated a radial distribution function (RDF) by averaging RDFs calculated for 50 snapshots of the equilibrated systems. The RDFs were calculated only for the atoms in the nanolayer. These RDFs were then compared to reference RDFs of the cop-

per fcc and copper glass systems. The short-range order of the amorphous nanolayers was analyzed using the Voronoi tessellation method implemented in OVITO,³² which divides the simulation cell into one polyhedron around each atom.^{33–36} The polyhedra are characterized by the Voronoi index $\langle n_3, n_4, n_5, n_6 \rangle$, where n_i denotes the number of i -edged faces of the polyhedron.

III. RESULTS

A. Mendelev potential

Figure 1 shows the time evolution of composite systems with different nanolayer thickness and the results of the CNA. Atoms depicted in yellow are nanolayer atoms that are fcc coordinated. On insertion, the nanolayer had a (100) surface orientation. We can see that the nanolayer with 3 ML of copper amorphizes after a short simulation time, while the copper with 5 ML thickness stays crystalline. At a thickness of 4 ML a mixed state occurs. The systems with different initial orientations show similar behavior.

For obtaining an independent confirmation of the appearance of an amorphous and crystalline copper phase at different nanolayer thicknesses, we calculated the RDFs of the nanolayers without including the glass matrix. The results are shown in Figure 2 and compared with the RDFs of the bulk crystalline and amorphous copper reference phases. Only three layers are shown for every initial surface orientation: the thickest amorphous layer, the thinnest crystalline layer, and the layer with a mixed state. The results match the CNA. Amorphous layers show a similar RDF to the bulk amorphous copper phase, including the characteristic double peak between 4 Å and 5 Å. The RDFs of completely crystalline layers match the bulk fcc copper, although the signal at large r gets smaller due to the finite size of the nanolayers. A mixed state is indicated by appearance of the second crystalline peak with reduced intensity. Depending on

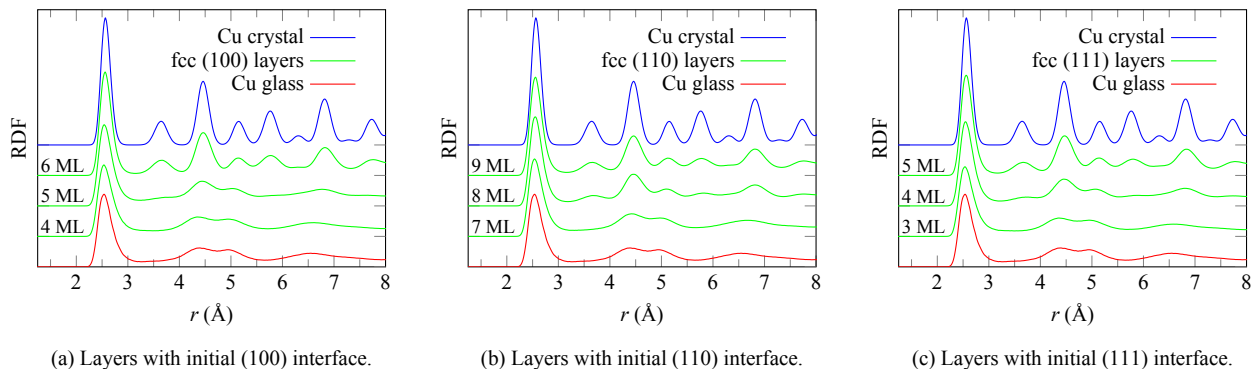


FIG. 3. Radial distribution functions of the copper nanolayers in several sandwich systems compared with the reference systems. Results of the simulation carried out using the Ward potential.

the fraction of the amorphous phase, the glass double peak starts separating into the two clearly distinct crystalline peaks (number three and four). In the system with initial (110) surface and a layer thickness of 5 ML, a small trace of crystalline phase is still detectable as indicated by a slight increase of the RDF at about 3.5 Å, the position of the second crystalline peak.

B. Ward potential

The simulations using the Ward potential show the same behavior as the simulations using the Mendelev potential. The corresponding RDFs of the copper nanolayers are shown in Figure 3. The RDFs exhibit the same characteristics, i.e., the gradual disappearance of the second crystalline peak as well as the appearance of the glass double peak with decreasing thickness. The amorphization also occurs in slightly thicker layers. For the system with an initial (100) surface, 4 ML are amorphous, and even the 5 ML system only shows a small amount of crystallization. The mixed state for the initial surfaces (110) and (111) appears at 8 ML and 4 ML, respectively. The CNA results agree with the RDFs and are comparable to Figure 1. They are therefore omitted here.

The simulations with both potentials agree that thin, initially crystalline nanolayers of copper become amorphous. Thus, we can already exclude that amorphization is a result of kinetics in the deposition process, as the layers were inserted in a crystalline state. Still, the creation of the interface may be connected with local heating, leading to a fast melt-quench process in the smaller layers. It is therefore necessary to investigate the thermodynamics of the system.

IV. MODEL

An indication for an energetically driven amorphization is already given by the fact that even initially crys-

talline nanolayers undergo a phase transformation to the amorphous state. To explain the amorphization of the nanolayers and to test the hypothesis of energetically driven SSA, we propose a simple thermodynamic model. We formulate the internal energy U of the composite systems. In the given ensemble, the free energy would be the appropriate thermodynamic potential, but given that the entropy term should favor the amorphization, we do not artificially increase the driving force for the amorphization, but rather underestimate it. The internal energy of a composite system with an embedded crystalline nanolayer is then

$$U_c = U_{MG} + Nu_{fcc} + 2A\gamma_{c-g}. \quad (1)$$

U_{MG} is the total internal energy of the bulk $\text{Cu}_{64}\text{Zr}_{36}$ glass phase, N is the number of atoms in the nanolayer, u_{fcc} is the internal energy per atom of the copper fcc crystal. Additionally, there are two interfaces, which contribute an energy of $A\gamma_{c-g}$ each, where A is the interface area.

If the system instead contains an embedded amorphous nanolayer, the internal energy is expressed as

$$U_a = U_{MG} + Nu_{am} + 2A\gamma_{g-g}, \quad (2)$$

where u_{am} is the per-atom internal energy of the glassy nanolayer and $A\gamma_{g-g}$ is the glass-glass interface energy.

Generally, it is to be expected that the internal energy of a copper crystal is lower than the internal energy of amorphous copper. As we nevertheless see amorphization of pure-metal nanolayers, the reason must lie in the interface energy. We propose that the crystal-glass interface energy γ_{c-g} is higher than the glass-glass interface energy γ_{g-g} . In that case an amorphous nanolayer must be energetically favorable if its thickness doesn't exceed a critical value, given that differences in interface energy can compensate the excess energy of the copper glass phase. A quantitative measure is provided by the internal energy difference, here expressed as an intrinsic

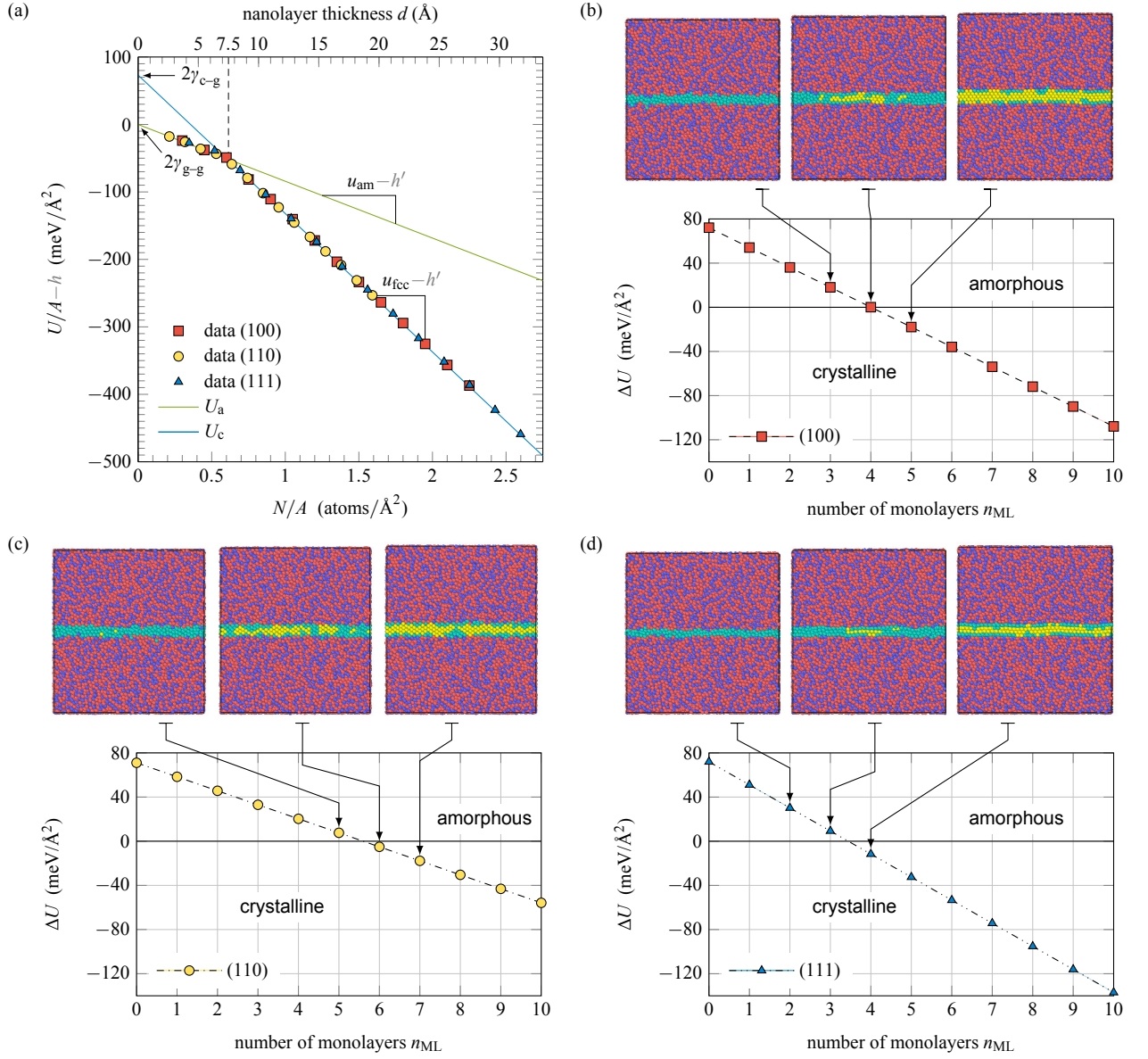


FIG. 4. Internal energies of the multilayer systems modelled with the Mendelev potential. (a) shows the internal energies extracted from the MD simulations as symbols and the linear regression results as lines. For visualization purposes a function $h = h' \cdot N/A$ with $h' = 3 \text{ eV}$ was subtracted to exaggerate the difference in slopes between U_c and U_a . In (b)–(d), ΔU is plotted as a function of the number of monolayers for initial surface orientations (100), (110), and (111). Additionally, snapshots of the MD simulation are added. Here, red and blue atoms are copper and zirconium, respectively. Green atoms are copper atoms belonging to the nanolayer. Yellow atoms are fcc coordinated.

quantity independent of the surface area:

$$\begin{aligned}
 \Delta U &= (U_c - U_a)/A \\
 &= \left(\frac{N}{A} u_{\text{fcc}} + 2\gamma_{\text{c-g}} \right) - \left(\frac{N}{A} u_{\text{am}} + 2\gamma_{\text{g-g}} \right) \\
 &= \frac{N}{A} \Delta u_{\text{Cu}} + 2\Delta\gamma.
 \end{aligned} \quad (3)$$

We can see that a negative value of ΔU signifies a stable crystalline nanolayer, while a positive value of ΔU

signifies a stable amorphous nanolayer:

$$\begin{aligned}
 \Delta U(N) < 0 & \quad \text{crystalline nanolayer} \\
 \Delta U(N) > 0 & \quad \text{amorphous nanolayer.}
 \end{aligned}$$

Should the theory hold, we should be able to show that the critical number of atoms N_{crit} at $\Delta U(N_{\text{crit}}) = 0$ is the same as observed in the simulation by CNA. To get a more descriptive quantity, the number of atoms can easily be converted to the number of monolayers n_{ML} or the thickness of the nanolayer d , as these quantities are

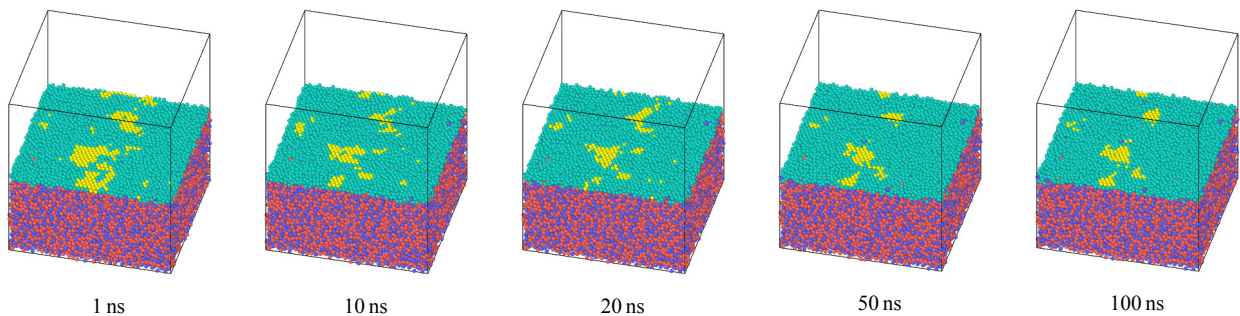


FIG. 5. Cut through a nanolayer of 3 ML thickness with an initial (111) surface at different time steps. Even after a simulation time of 100 ns, the mixed crystalline/amorphous state stays stable. The simulation was carried out using the Mendelev potential. Copper and zirconium atoms are shown in red and blue, respectively. Copper atoms belonging to the nanolayer are yellow if they are fcc coordinated and green otherwise.

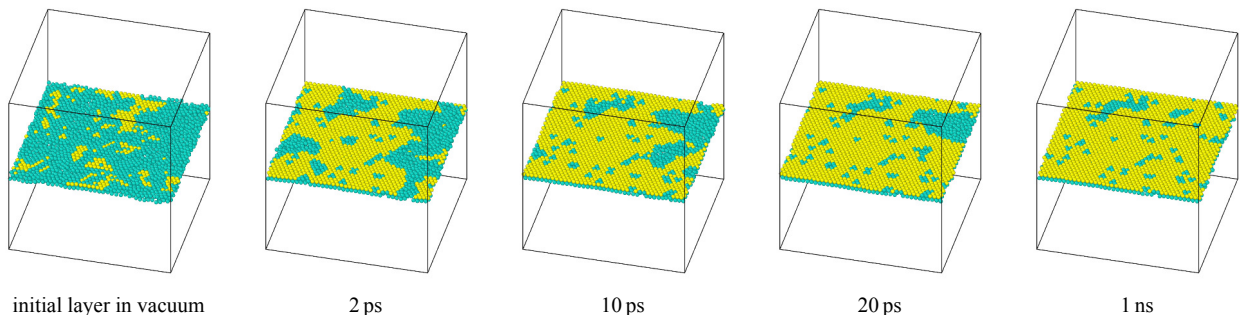


FIG. 6. The nanolayer shown in Figure 5 removed from the metallic glass matrix and put in vacuum. The cut shows that the layer crystallizes almost immediately, proving that only the glass-glass interface stabilizes the amorphous phase. Yellow atoms are fcc coordinated.

proportional:

$$\frac{N}{A} \propto n_{\text{ML}} \propto d.$$

The missing parameters in our model are now u_{fcc} , u_{am} , $\gamma_{\text{c-g}}$, and $\gamma_{\text{g-g}}$. Using equations 1 and 2, the internal energies of the different layer phases can be obtained from the relations

$$u_{\text{fcc}} = \frac{dU_{\text{c}}}{dN} \quad \text{or} \quad u_{\text{am}} = \frac{dU_{\text{a}}}{dN}, \quad (4)$$

respectively. Alternatively, it would be conceivable to just use the internal energies of the bulk copper reference systems. The problem would be that the amorphous phase in the nanolayer is not necessarily the same as in the bulk. The bulk amorphous copper is quenched with very high cooling rates and has therefore more similarity to the melt. The amorphous copper phase in the nanolayer may exhibit different short-range order as it is allowed to relax to a low-energy state. Furthermore, the ratio of interface to volume is very high, which means that the nanolayer structure is highly influenced by interface contributions. To calculate the interface energy, the internal energy U_{MG} is first taken from the pure $\text{Cu}_{64}\text{Zr}_{36}$ glass sample before embedding the copper

nanolayer. This allows to calculate the interface energies either by directly using equations 1 and 2, or by subtracting U_{MG} from the U -axis intercept of the $U(N)$ curves. Both should yield the same result. We assume here that the interface energy is constant, see 29, section II for proof.

A. Mendelev potential

Figure 4a shows the internal energies U_{c} and U_{a} as a function of the number of atoms. All values are normalized to the interface area and U_{MG} is already subtracted. The symbols show the internal energies extracted from the MD simulation, while the lines show the linear regression. The numerical data is listed in Table I. We note that all crystalline nanolayers have (approximately) the same interface energy in the Mendelev potential. The graph shows that the glass-glass interface energy is lower than the crystal-glass interface (in fact it is zero, which will be discussed in detail in section V), which fits the assumptions of our model. This lowered $\gamma_{\text{g-g}}$ favors a glassy nanolayer up until approximately $0.6 \text{ atoms}/\text{\AA}^2$, which corresponds to a critical thickness of about

$$d_{\text{crit}} \approx 7.5 \text{ \AA}. \quad (5)$$

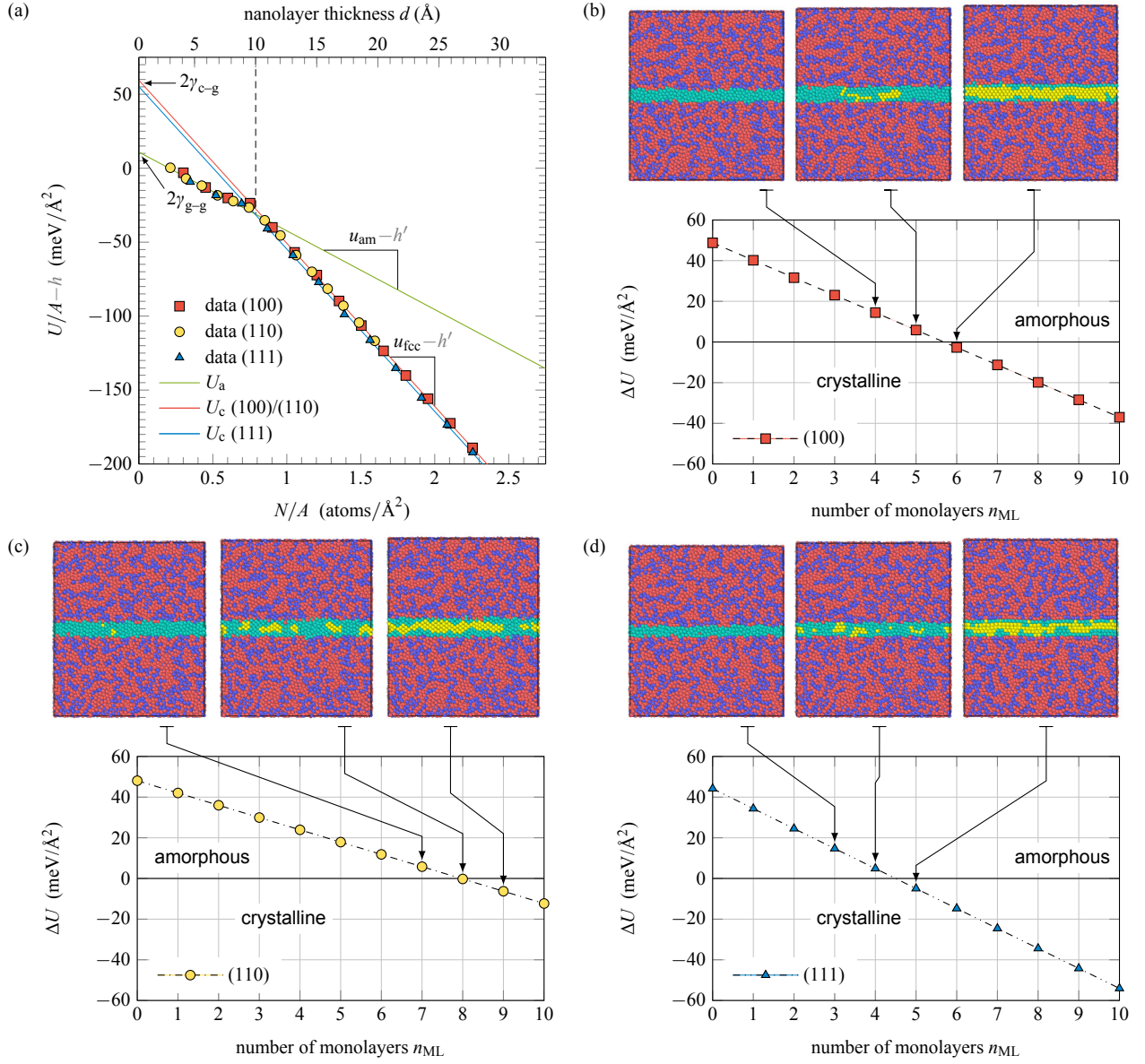


FIG. 7. Internal energies of the multilayer systems modelled with the Ward potential. (a) shows the internal energies extracted from the MD simulations as symbols and the linear regression results as lines. For visualization purposes a function $h = h' \cdot N/A$ with $h' = 3.35$ eV was subtracted to exaggerate the difference in slopes between U_c and U_a . In (b)–(d), ΔU is plotted as a function of the number of monolayers for initial surface orientations (100), (110), and (111). Additionally, snapshots of the MD simulation are added. Here, red and blue atoms are copper and zirconium, respectively. Green atoms are copper atoms belonging to the nanolayer. Yellow atoms are fcc coordinated.

The thickness d_{crit} can only be given approximately, due to the different densities of the two phases and the rough interface. Figures 4b–d show ΔU as a function of the number of monolayers. The direct comparison reveals that the calculated energy differences and the solid-state amorphization observed by the CNA method agree very well. At the critical thickness $\Delta U = 0$ we observe a mixed crystalline/amorphous nanolayer. The figures show that the transition is not as sharp as our model assumes, a partly crystalline layer also exists for ΔU slightly greater

than zero. That is a result of omitting a description of the two-phase region in the model; entropy and the additional interfaces play a role here. Nonetheless, the critical thickness is correctly reproduced without these complications. A further comparison with the RDFs in Figure 2 leads to the same conclusions. While the good fit of the model with simulation data supports the conclusion that the SSA is due to energetic reasons, we also investigated the influence of the simulation setup on the amorphization of the nanolayers in 29, section III. We

find that the interface creation leads to a heat spike, but that this only serves as activation energy for the SSA process. Crystalline layers with a thickness below d_{crit} can be produced, but are not energetically favorable.

In order to verify that the amorphous phase is indeed stable over a long time scale and that this is a result of the glass–glass interface, we conducted two further simulations. In the first simulation, we simply took a composite system with a mixed crystalline/amorphous state in the copper nanolayer and let the simulation run for 100 ns. If the amorphous phase is only produced by, e.g., stress in the initial system after insertion of the nanolayer, the crystalline phase should start growing again over the longer time frame. The simulation results are depicted in Figure 5 and show that the mixed state is stable, as predicted by our model.

A direct proof that the solid-state amorphization is due to the presence of a glass–glass interface was obtained by removing the glass matrix. The results are shown in Figure 6. The free amorphous layer crystallizes almost immediately, as would be expected.

B. Ward potential

Figure 7a shows the internal energies as calculated with the Ward potential as a function of the number of atoms. All values are again normalized to the interface area and U_{MG} is already subtracted. The symbols show the internal energies extracted from the MD simulation, while the lines show the linear regression. In the Ward potential the (111) interface has a slightly lower interface energy than the (100) and (110) interfaces, which are approximately the same (see also Table I). As with the Mendelev

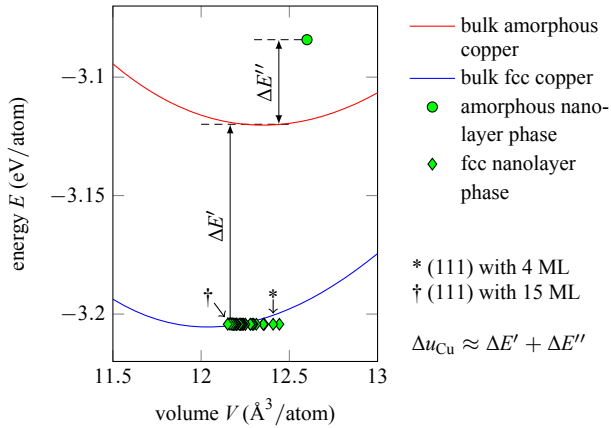


FIG. 8. Energy–volume curves for amorphous and crystalline copper and data points for amorphous and crystalline nanolayers. Atomic volumes of the nanolayers were obtained by a Gauss fit to the Voronoï volume distribution. The crystalline nanolayers vary in density with their thickness, approaching the equilibrium volume of an fcc crystal at higher thickness.

potential, the glass–glass interface energy is lower than the crystal–glass interface energy, favoring an amorphous nanolayer up to the critical thicknesses

$$d_{\text{crit}}^{(100)} \approx 10.8 \text{ \AA}, \quad (6)$$

$$d_{\text{crit}}^{(110)} \approx 10.7 \text{ \AA}, \text{ and} \quad (7)$$

$$d_{\text{crit}}^{(111)} \approx 9.9 \text{ \AA}. \quad (8)$$

The difference in critical thickness is a result of different $\gamma_{\text{c-g}}$ for the three surface orientations. The transition thickness is higher than in the Mendelev potential despite a smaller $\Delta\gamma$, as the excess energy of the amorphous phase is lower. By plotting ΔU as a function of the number of monolayers, a direct comparison to CNA and RDF results is possible. Figures 7b–d show $\Delta U(n_{\text{ML}})$ compared with snapshots from the simulation. Again, a good match between the nanolayer phases shown in the snapshots and the predicted critical thickness is visible. For the same reasons as stated earlier, a mixed state occurs.

All in all, the results using both potentials agree qualitatively and support our thermodynamic model. Therefore, a purely kinetic reason for the amorphous nanolayers can be ruled out and an energetic picture of solid-state amorphization can be supported.

V. STRUCTURE AND ENERGY

A. Mendelev

We compared the energy of the amorphous nanolayer copper phase with the reference bulk amorphous copper phase. The energy–volume curve in Figure 8 shows that the nanolayer phase is energetically higher than the bulk phase. Additionally, an expansion of the crystalline layer at low thicknesses is visible, possibly due to interface stress. Both the peculiarity of the zero glass–glass interface energy, as well as the higher excess energy of the amorphous phase can be linked to the structure of the phase. Figure 9a shows the Voronoï statistics of those copper atoms in the nanolayer, that are only surrounded by other copper atoms. This allows a comparison to bulk amorphous copper: in contrast to the bulk phase, the nanolayer phase contains no twelve-fold coordinated atoms. This higher energy structure is stabilized by the interface, as shown in Figure 9b: the Voronoï statistics of the whole nanolayer (including copper atoms that have zirconium neighbors) are very similar to the bulk $\text{Cu}_{64}\text{Zr}_{36}$. This reduces the interface energy to almost zero.

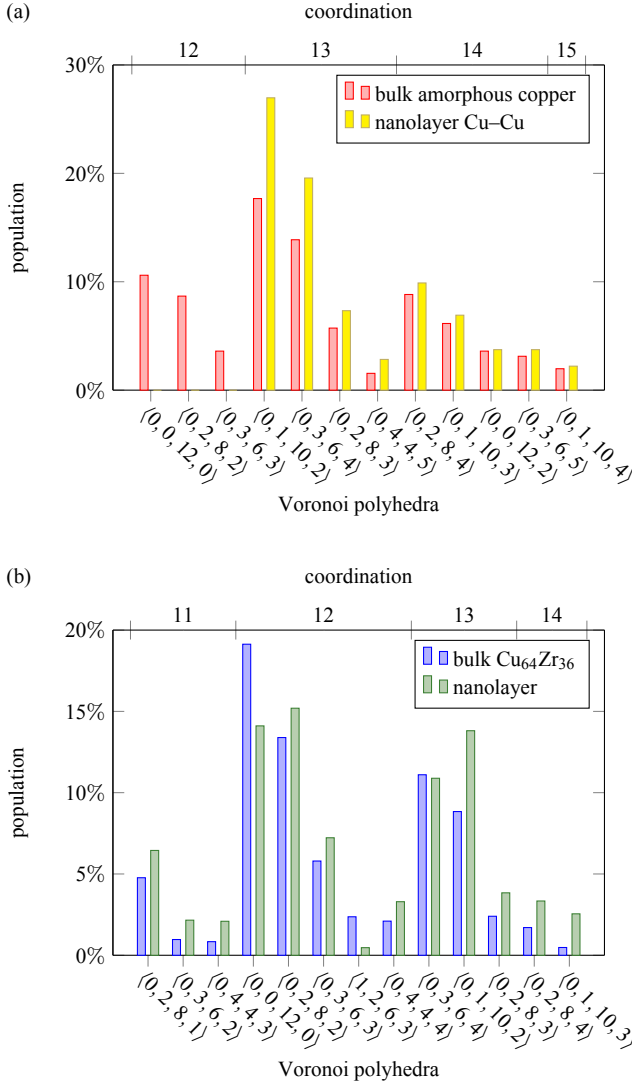


FIG. 9. Voronoi analysis of the amorphous nanolayers in systems simulated using the Mendelev potential. In (a) the bulk amorphous copper phase is compared with the amorphous copper phase in the nanolayers. Only those nanolayer atoms were included, which were surrounded solely by other copper atoms. In (b) all nanolayer atoms (including those with zirconium neighbors) were considered and compared to $\text{Cu}_{64}\text{Zr}_{36}$ bulk.

B. Ward

In the Ward potential the amorphous nanolayer also features a structure with different energy than the bulk amorphous copper (-3.39 eV/atom for the reference system, -3.40 eV/atom for the amorphous nanolayer). The explanation can again be found in the Voronoi statistics of nanolayer copper atoms surrounded completely by other copper atoms: Figure 10a shows that the twelve-fold coordinated atoms are missing again. The comparison of the Voronoi statistics of the whole nanolayer, though, show a difference to the $\text{Cu}_{64}\text{Zr}_{36}$ MG, especially

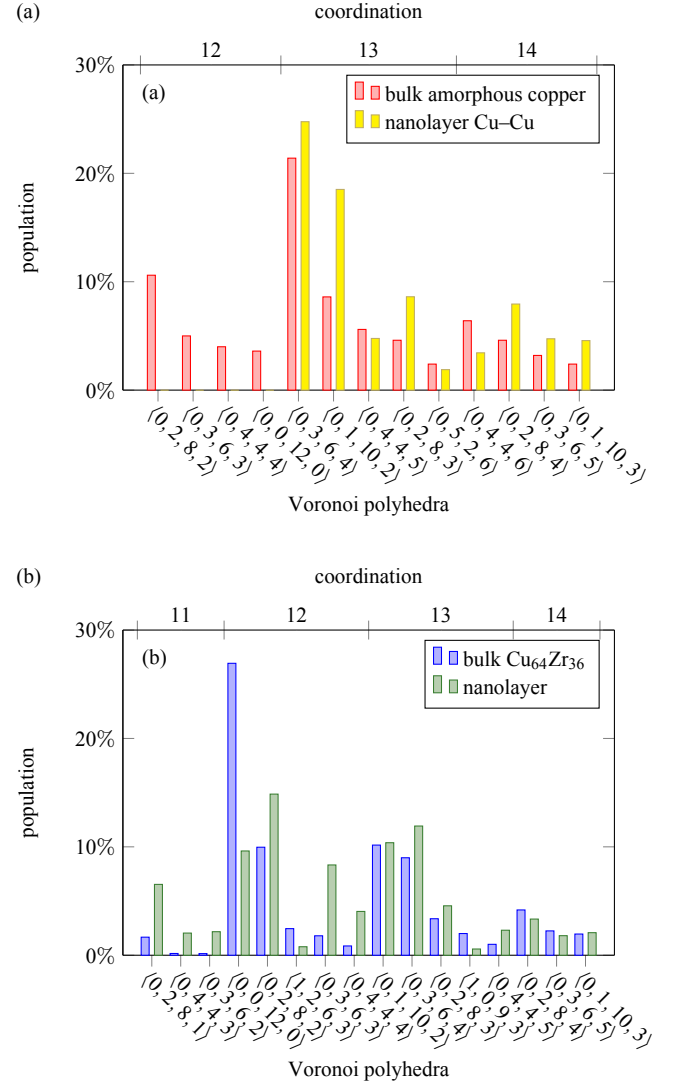


FIG. 10. Voronoi analysis of the amorphous nanolayers in systems simulated using the Ward potential. In (a) the bulk amorphous copper phase is compared with the amorphous copper phase in the nanolayers. Only those nanolayer atoms were included, which were surrounded solely by other copper atoms. In (b) all nanolayer atoms (including those with zirconium neighbors) were considered and compared to $\text{Cu}_{64}\text{Zr}_{36}$ bulk.

concerning the $\langle 0,0,12,0 \rangle$, $\langle 0,2,8,2 \rangle$, and $\langle 0,3,6,3 \rangle$ polyhedra (Figure 10b). This leads to a small but non-zero glass-glass interface energy.

VI. CONCLUSIONS

Using MD simulations, we observed the amorphization of elemental copper nanolayers embedded in a $\text{Cu}_{64}\text{Zr}_{36}$ metallic glass if the layer thickness stays below a critical value. This is in accordance with experimental results, which report thin amorphous iron nanolayers embedded

TABLE I. Internal energies and interface energies extracted from MD simulations and predicted critical thicknesses.

Potential	Initial interface	u_{fcc}	u_{am}	Δu_{Cu}	γ_{c-g}	γ_{g-g}	$\Delta\gamma$	N_{crit}/A	d_{crit}
			(eV/atom)			(meV/Å ²)		(atoms/Å ²)	(Å)
Mendelev	(100)	-3.20	-3.08	-0.12	36.5	0.4	36.1	0.601	7.5
	(110)	-3.20	-3.08	-0.12	35.5	0.1	35.4	0.592	7.5
	(111)	-3.20	-3.08	-0.12	36.0	-0.5	36.5	0.606	7.5
Ward	(100)	-3.46	-3.40	-0.06	29.7	5.4	24.4	0.855	10.8
	(110)	-3.46	-3.40	-0.06	29.5	5.5	24.0	0.846	10.7
	(111)	-3.46	-3.40	-0.06	27.6	5.5	22.1	0.781	9.9

in Co₇₅Fe₁₂B₁₃.²² We could show that the amorphization is not a kinetic effect due to deposition, as our simulations start from a crystalline state. Rather, the glass–glass interface energy is significantly lower than the crystal–glass interface energy, which stabilizes the amorphous copper phase. This solid-state amorphization is similar to the case at heterogeneous crystal interfaces, except that in our case the reduced glass–glass interface energy is sufficient to induce amorphization. At a critical layer thickness, which is on the order of a nanometer, a mixed crystalline/amorphous state appears. This state is also stable over longer times, which further supports the picture of solid-state amorphization: if the amorphous state is only a result of stresses in the initial setup, the crystallites in the layer would grow again with time. They instead keep their size. Analysis of the amorphous structure in the nanolayer further confirms that the interface energy is a dominating factor in the structure of thin nanolayers: if it can be reduced, the amorphous layer can even be driven into a state with a higher bulk energy than

a quenched melt. Technological applications for glass–glass composite systems have already been proposed in the realm of magnetic tunnel junctions^{22,37} and could benefit from further research into different multilayer systems.

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* brink@mm.tu-darmstadt.de

† Present address: IFW Dresden, P.O. Box 270116, D-01171 Dresden, Germany

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Supplemental Material on the Simulation Setup

Solid-state amorphization of Cu nanolayers embedded in a $\text{Cu}_{64}\text{Zr}_{36}$ glass

This supplemental material discusses some additional technical aspects of the simulation setup in detail. In the first section, we show that the systems are equilibrated. We demonstrate in the second section that the interface energy is a constant independent of the layer thickness. In the final section, we discuss the kinetics during interface creation and show that they do not influence the thermodynamics of the system.

I. EQUILIBRATION OF GLASS MATRIX AND COMPOSITES

To extract the correct energies from the molecular dynamics (MD) simulations, it is necessary to make sure

that the systems are equilibrated, i.e., that the energy of the system is constant in time. The composites were equilibrated for 1 ns at 300 K, which is sufficient to equilibrate the composite systems. This is shown exemplarily for the Mendelev potential, for systems with initial (100)

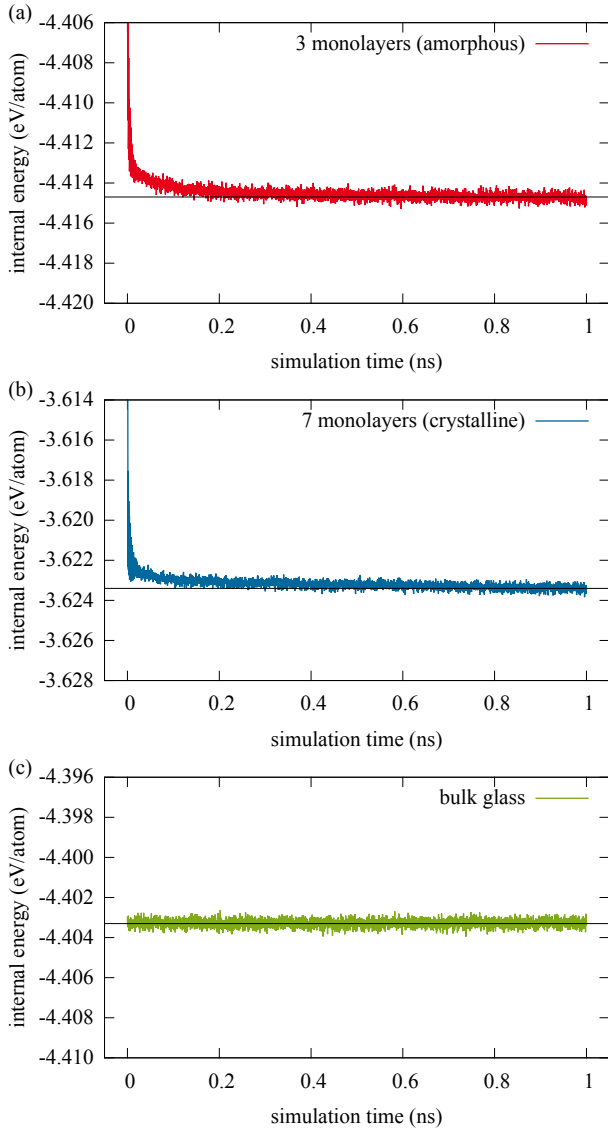


FIG. 1. Internal energy over time for systems simulated with the Mendelev potential. (a–b) Internal energy of two metallic glass–copper composite systems. (c) Internal energy of the pure metallic glass.

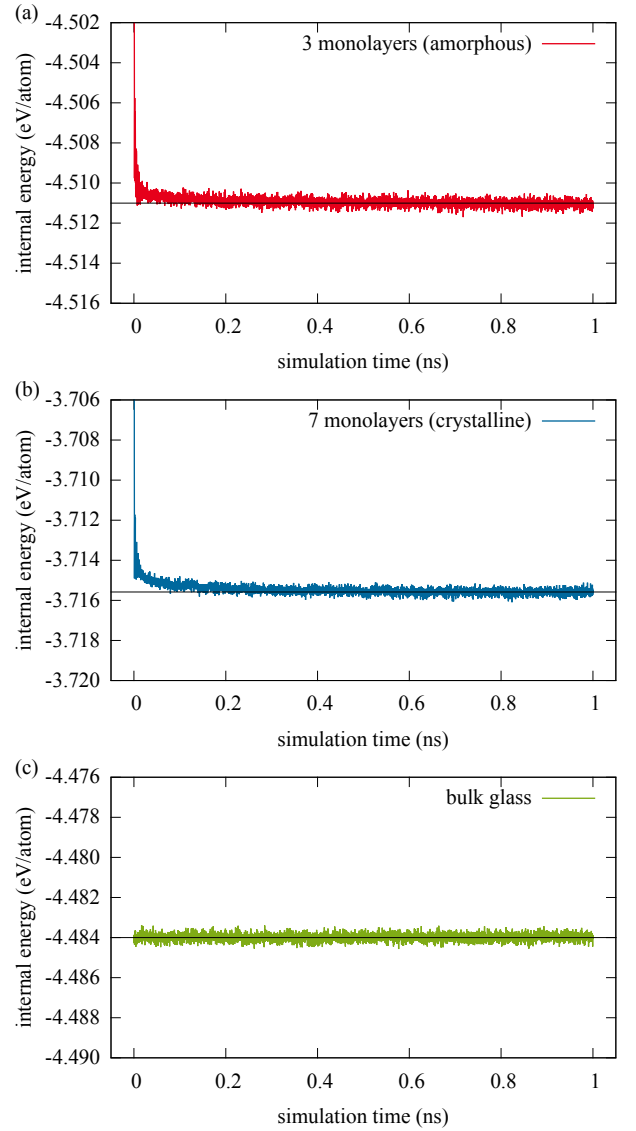


FIG. 2. Internal energy over time for systems simulated with the Ward potential. (a–b) Internal energy of two metallic glass–copper composite systems. (c) Internal energy of the pure metallic glass.

interface and 2 monolayers of copper (Figure 1a), as well as 15 monolayers of copper (Figure 1b). For the Ward potential, the same is shown in Figures 2a and 2b. To ensure that the energy of the glass matrix stays constant over the simulation time, we ran simulations with only the glass matrix for 1 ns. These are shown in Figures 1c and 2c and show that the glass is already equilibrated and does not change in internal energy.

II. INDEPENDENCE OF THE INTERFACE ENERGY FROM LAYER THICKNESS

Our model assumes an interface energy independent of the layer thickness. To prove that this assumption is correct, we additionally performed simulations on a system with 100 monolayers of copper using the Mendelev and the Ward potential. We inserted the results of this simulation into plots of the internal energy as a function

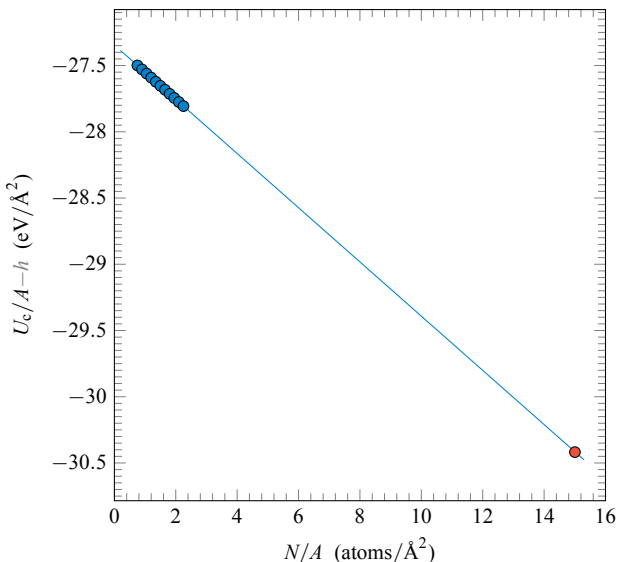


FIG. 3. Internal energy over number of atoms for crystalline nanolayers with initial (100) surface in the Mendelev potential. The blue circles show the results from Figure 4a in the main paper. The red circle is the system with 100 monolayers of copper. To exaggerate the slope for visualization purposes, we subtracted a function $h = 3 \text{ eV} \cdot N/A$ from U/A .

TABLE I. Comparison of the interface energy in a composite system with initial (100) surface modelled using the Mendelev potential.

	u_{fcc} (eV/atom)	$U_{\text{MG}}/N_{\text{MG}}$ (eV/atom)	$\gamma_{\text{c-g}}$ (meV/Å ²)
5–15 layers	−3.20	−4.40	36.5
100 layers	−3.20	−4.40	35.6

of the number of layer atoms, both normalized to the interface area. Figures 3 and 4 show that the composites with very big copper layers have the same energy U_c as predicted by extrapolation using our model (line). Furthermore, we calculated u_{fcc} for the copper nanolayer atoms far from the interface, as well as the per-atom energy of the metallic glass matrix far from the interface and compared them to the values from Table I in the main paper. Tables I and II list the results and clearly show that the results in a system with “bulk” copper agree with the results for composites with thin copper layers. The small deviation of the interface energy, as well as the deviation of U_{MG} for the Ward potential, lie inside the range of numerical errors. The independence of the interface energy from the layer thickness is already a reasonable assumption, given the linear behavior of U_c and U_a . With these additional data, the assumption is proven.

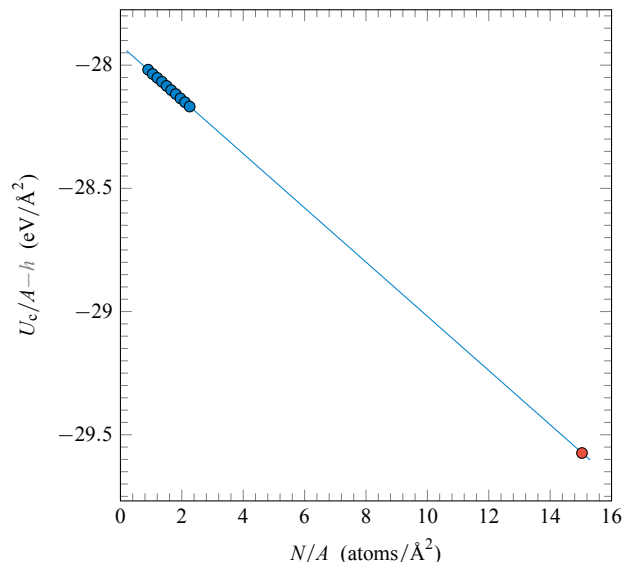


FIG. 4. Internal energy over number of atoms for crystalline nanolayers with initial (100) surface in the Ward potential. The blue circles show the results from Figure 7a in the main paper. The red circle is the system with 100 monolayers of copper. To exaggerate the slope for visualization purposes, we subtracted a function $h = 3.35 \text{ eV} \cdot N/A$ from U/A .

TABLE II. Comparison of the interface energy in a composite system with initial (100) surface modelled using the Ward potential.

	u_{fcc} (eV/atom)	$U_{\text{MG}}/N_{\text{MG}}$ (eV/atom)	$\gamma_{\text{c-g}}$ (meV/Å ²)
6–15 layers	−3.46	−4.48	29.7
100 layers	−3.46	−4.49	29.3

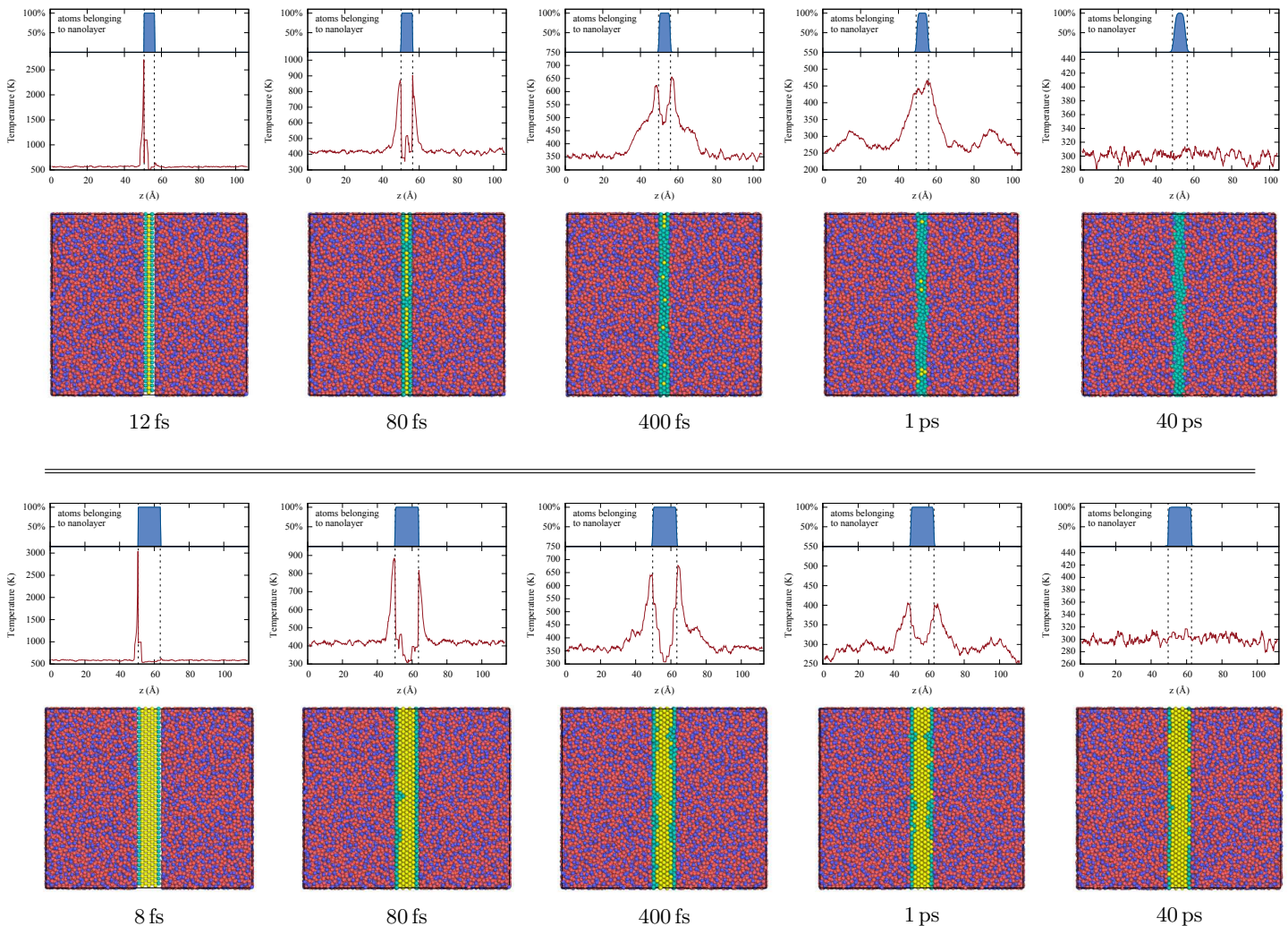


FIG. 5. Temperature profiles for composite systems simulated using the Mendelev potential. The top row shows a system with 3 monolayers, the bottom row a system with 7 monolayers of copper. The graphs are produced by averaging over 2 Å thick slices, of which there are 500 in z direction. The top part of the graphs show the ratio of layer atoms to matrix atoms in the current slice to indicate the position of the two phases and their interface. The lower part of the graphs show the temperature in the current slice. Below the graphs, the corresponding snapshots of the composite systems are shown. The leftmost snapshots are always from the simulation step with the highest temperature spike. *Note:* After creating the composite systems, we initialize the momenta from a Maxwell-Boltzmann distribution. For the first few steps the distribution between kinetic and potential energy is not equilibrated, which leads to an instantaneous temperature higher than 300 K in the glass matrix.

III. CREATION OF THE COMPOSITE SYSTEMS AND KINETICS AT THE INTERFACE

After inserting the copper nanolayers, some atoms from the nanolayer may have a small distance to atoms from the metallic glass matrix. This could lead to a high potential energy and consequently initial temperature spikes at the interfaces, which may be responsible for the amorphization of the nanolayers. In fact, for some time at the beginning of the simulation, temperature spikes appear mainly on the matrix side of the interface (Figures 5 and 6). In case of the systems with nanolayers thick enough to stay crystalline, the temper-

ature inside of the layer stays comparatively low, while there is an increase of temperature in the layers when they become amorphous. While this may be a sign of the amorphous phase being the result of a fast melt-quench process, it may also be that the initial heat spike only provides an activation energy for an energetically favorable solid state amorphization. To test this, we used a modified simulation setup: The system was prepared in the same way as described in the main paper, but the nanolayers were held fixed in the crystalline state for 1 ns. This avoids penetration of heat into the layer. After that, the nanolayers were released and the whole system equilibrated normally for an additional 1 ns. Additionally, we

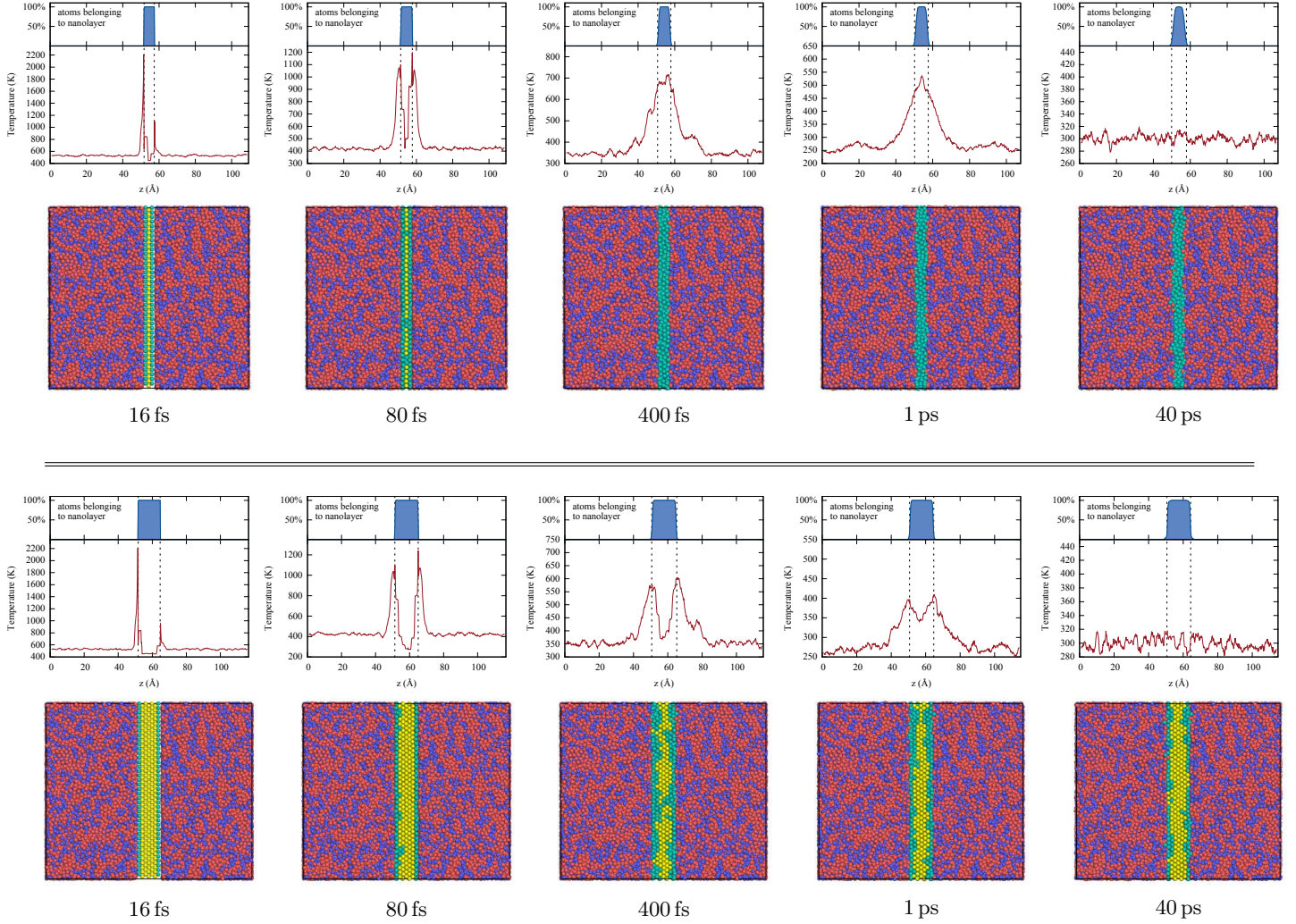


FIG. 6. Temperature profiles for composite systems simulated using the Ward potential. The top row shows a system with 3 monolayers, the bottom row a system with 7 monolayers of copper. The graphs are produced by averaging over 2 Å thick slices, of which there are 500 in z direction. The top part of the graphs show the ratio of layer atoms to matrix atoms in the current slice to indicate the position of the two phases and their interface. The lower part of the graphs show the temperature in the current slice. Below the graphs, the corresponding snapshots of the composite systems are shown. The leftmost snapshots are always from the simulation step with the highest temperature spike.

ran molecular statics simulations on the initial system, which also avoids heating the system locally. The results are shown in Figures 7 and 8. The molecular statics simulations never lead to an amorphization of the copper layer. The reason for that is simply that a phase transformation from fcc copper to amorphous copper needs a certain activation energy. We can also see that the energy of the statically relaxed systems is always much higher than the MD-equilibrated systems. This shows that even the creation of a low-energy crystal–glass interface needs some activation energy. When holding the copper layers fixed, very small layers will still become amorphous, while the amorphization is suppressed in thicker layers. These crystalline nanolayers are metastable, as can be seen in the graphs: Their energy agrees with the prediction of

our model (blue line), which also states that $\Delta U > 0$ in this case. Only above the critical thickness, at the crossover of U_a (dashed line) and U_c (blue line), are the crystalline nanolayers stable again. This is in complete agreement with our model and shows that initially fixing the copper layers only kinetically inhibits the phase transformation on the simulated time scales.

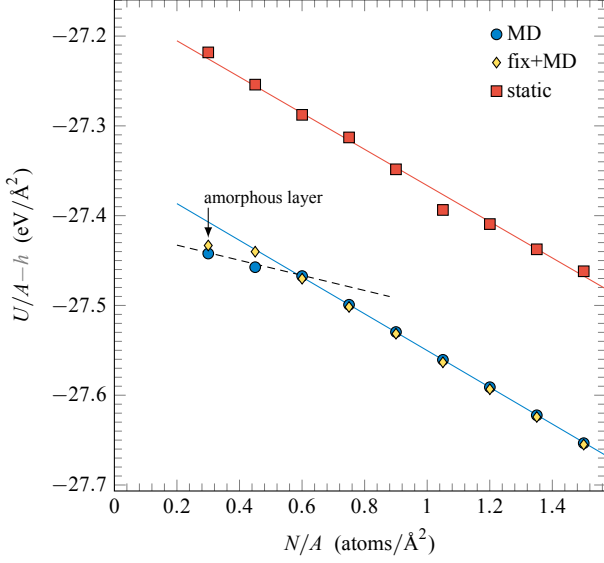


FIG. 7. Internal energy of the composite systems as a function of the number of atoms in the nanolayer. This graph shows nanolayers with initial (100) surface in the Mendelev potential. Data was normalized to the interface area and a function $h = 3 \text{ eV} \cdot N/A$ was subtracted from U/A to exaggerate the difference in slopes for visualization purposes. The blue circles show the results from Figure 4a in the main paper. The yellow diamonds show the results of an MD simulation where the layer atoms are first held in position, followed by a normal MD simulation. Except where marked, the nanolayers stayed crystalline in these simulations. Red squares show a simple molecular statics calculation plus a $2 \times \frac{3}{2} N k_B T$ term, to compensate for the missing temperature contribution to the internal energy.

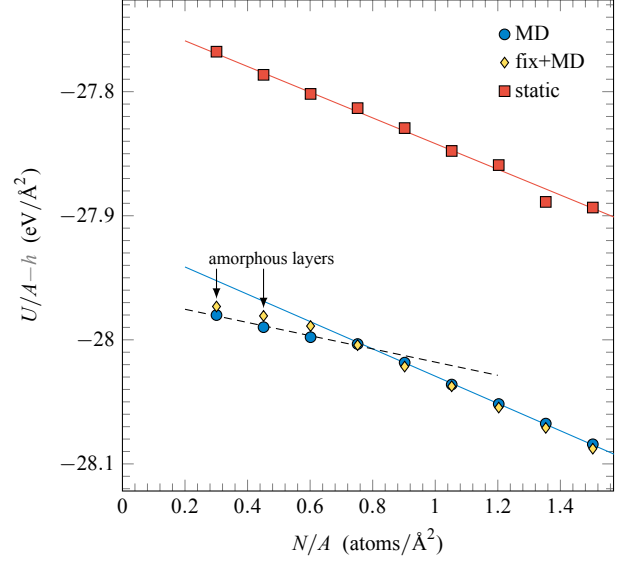


FIG. 8. Internal energy of the composite systems as a function of the number of atoms in the nanolayer. This graph shows nanolayers with initial (100) surface in the Ward potential. Data was normalized to the interface area and a function $h = 3.35 \text{ eV} \cdot N/A$ was subtracted from U/A to exaggerate the difference in slopes for visualization purposes. The blue circles show the results from Figure 7a in the main paper. The yellow diamonds show the results of an MD simulation where the layer atoms are first held in position, followed by a normal MD simulation. Except where marked, the nanolayers stayed crystalline in these simulations. Red squares show a simple molecular statics calculation plus a $2 \times \frac{3}{2} N k_B T$ term, to compensate for the missing temperature contribution to the internal energy.